## FORMAL MODELING

#### **How to Write a Mathematical Article**



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## Some general remarks

- Every author has her/his own style and preferences how to write an article.
- The structure strongly depends on the topic/message of the article.
- ⇒ There is no final word how one should write a mathematical article...

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# The outline

1. The general form using latex (with the LNCS-style)

Some (hopefully) useful remarks (based on my experience):

- 2. How to write the mathematical content (just math!)
- 3. Presenting the main content (with explanations)
- 4. General/personal hints/tips

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```
\documentclass[english, runninghead, a4paper]{llncs}
... %What ever you need...
\begin{document}
```

#### The document style

- Each journal/conference proceeding has its own style whose rules one should/must follow.
- Warning: proceedings often have rigorous page limits!
- However, the structure (up to some technical details) is always the same.
- In the *PS Formal Modelling* we require the Springer style LNCS.

```
ftp://ftp.springernature.com/cs-proceeding/llncs/llncs2e.zip
```

```
\title{Find a catchy titile\thanks{Supported by the Austrian FWF....}}
```

#### The title

- The first hurdle: 90% of the potential readers will check only the title.
- A good title should
  - □ be simple and direct;
  - be attractive and informative;
  - contain the most important keywords;
     (domain/objects, problem/theorem/conjecture, solution/method);
  - □ not be too long or too short (or cryptic);
  - □ avoid nonstandard abbreviations and unnecessary acronyms.
- Often the funding agency (e.g. the Austrian FWF) is mentioned via a footnote.

```
\author{Carsten Schneider}
\institute{Research Institute for Symbolic Computation (RISC)\\
    Johannes Kepler University Linz\\ Altenberger Str.\ 69, 4040 Linz, Austria\\
    \email{cschneid@risc.jku.at}
}
\maketitle
```

The author(s) and the institution(s) with email(s)

```
\begin{abstract}
    The abstract should briefly summarize the contents; 150-250 words.
    \keywords{First keyword \and Second keyword \and Another keyword.}
\end{abstract}
```

#### The abstract (and keywords)

- The second hurdle: Among the 10% who passed the title 90% will quit after reading the abstract.
- Just plain text: avoid formulas, citations, and references to the text below.
- Simple sentences, avoid technical words (for the non-expert).
- Why should the reader continue reading: explain what you advertised with the title. What is special?
- Summarize the main content/message of the article.

\section{Introduction}

#### The introduction (1–2 pages $+\epsilon$ )

- The final hurdle: Among the remaining readers only 10% will proceed...
- It should present the state-of-the-art citing relevant/related work.
- It should connect the content of this article with the known results
- It should specify the main result:
  - □ ideally, a precise statement/specification/problem description;
  - □ if too complicated, a simplified version in prose;
  - □ if possible, a concrete (short!) example to illustrate the result.
- The last paragraph should sketch the outline of the remaining sections:

The outline of the article is as follows. In Section~\ref{Sec:NextSection} the basic definitions and the detailed problem description is given.... The conclusion is given in Section~\ref{Sec:Conclusion}.

```
\section{Further sections...}
```

#### The main content

- The structure depends on the concrete context/the preferences of the author.
- Some hints will be given later...

We follow the definitions given in~\cite{PS:19}.

■ Of great help are environments (available in LNCS):

```
\text{\left\text{begin(definition)\label{Def:DR}}} A difference ring \text{\set A,\sigma)\text{\set A\to\set A\text{\set aring \text{\set A\to\set A\to\set A\text{\set A\to\set A\to\s
```

■ and macros (see, e.g., https://arxiv.org/)

\section{Conclusion}

#### The conclusion

- It summarizes the main results of the article (extra notions are allowed that occur within the main text).
- However, readers might jump directly from the introduction to the conclusion. Thus avoid too many technical words.
- An outlook is given. E.g., the following questions can be addressed:
  - □ What can be done next?
  - What are possible (future) applications?
  - □ Are there conjectures/unanswered problems?
  - How can the presented ideas be generalized/extended?

\subsubsection\*{Acknowledgements} I would like to thank ...

#### The acknowledgment

- This part is optional.
- If appropriate, one can thank
  - □ colleagues (advisors) for fruitful discussions;
  - referees for careful reading and valuable comments;
  - □ funding agencies (if the thanks command in the title is excluded).

\documentclass[english, runninghead, a4paper]{|lncs| ... %define macros/load extra packages... \begin{document} \title{Find a catchy titile\thanks{Supported by the Austrian FWF....}} \author{Carsten Schneider} \institute{Research Institute for Symbolic Computation (RISC)\\ Johannes Kepler University Linz\\ Altenberger Str.\ 69, 4040 Linz, Austria\\email{cschneid@risc.iku.at}} \maketitle \begin{abstract} The abstract should briefly summarize the contents: 150-250 words. \keywords{First keyword \and Second keyword \and Another keyword.} \end{abstract} \section{Introduction}\label{Sec:Introduction} \section{Further sections...}\label{Sec:NextSection} \section{Conclusion}\label{Sec:Conclusion} \subsubsection\*{Acknowledgements} I would like to thank ... \bibliographystyle{splncs04} \bibliography{mybibliography} \appendix \section{Appendix} \section{Appendix 2}

\end{document}

```
\bibliographystyle{splncs04}
\bibliography{mybibliography}
\end{document}
```

#### The bibliography

■ Store all bib-items in mybibliography.txt. E.g.,

```
@incollection {PS:19,
AUTHOR = {Paule, Peter and Schneider, Carsten},
TITLE = {Towards a symbolic summation theory for unspecified sequences},
BOOKTITLE = {Elliptic integrals, elliptic functions and modular forms inquantum field theory},
SERIES = {Texts Monogr. Symbol. Comput.},
PAGES = {351-390},
PUBLISHER = {Springer, Cham},
YEAR = {2019}
```

- Bib-items can be copied from many places:
  - □ https://mathscinet.ams.org/mathscinet/index.html
  - □ https://dblp.uni-trier.de/
  - □ https://zbmath.org/authors/

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\end{document}

```
\appendix
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...
```

#### The appendix

- This part is optional.
- Depending on the convention, it can be put before or after the bibliography.
- Move aspects to the appendix that would destroy the main flow of the article, but which are relevant for the interested reader. Typical examples are:
  - ☐ A detailed proof of a statement that is needed in the article (but which is irrelevant to understand the main result).
  - □ A detailed example/demo.
  - □ Further aspects that are related but that do not fit directly to the main topic.

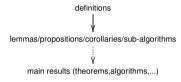
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### 2. How to write the mathematical content (just math!)

[Note: here you see my personal opinions/experiences]

1. First produce correct mathematics in bottom-up style:



- 2. Afterwards check (and, if necessary, go back to 1):
  - □ correctness:
  - completeness:
    - Are there details missing in the proof?
      - → Maybe an extra lemma is in place?
    - Can one easily generalize some results (without extra pain)?
    - Are all notions properly defined?
      - → Insert extra definitions...
  - □ Can one simplify the proofs?
    - · Often the definitions are clumsy.
    - · Being slightly less general might simplify the proofs dramatically.

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There are two main approaches.

- proof oriented: bottom-up construction
   definitions → lemma → ... → lemma/proposition → main theorems/algorithms
- reader friendly: top down construction
   problem specification → theorem → lemma/proposition → ... → basic constructions/definitions

The reader should be motivated: why do we need all these technical proofs/constructions to obtain the main result?

Problem: (1) is rather technical, but (2) is often not feasible.

Often the following combined/hybrid version (or variants of it) is appropriate:

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Rather time consuming, but it pays off (concerning readability):

# Construct one (or more) running example(s) that illustrate the full construction

- it should be compact but not trivial (the highlights/results of the article must be illustrated);
- it should start with the basic definitions and end, e.g., with the output of your algorithm. 28/30

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    - just parse formulas for syntactical correctness (brackets etc);
    - · read the text but ignore formulas;
    - · compare related formulas and check inconsistencies;
    - check if all objects are defined when they arise the first time;
    - check if all existing results are properly cited;
    - · check the citation list (spelling);
    - · check if you cited all articles that are relevant;

... 30/30